Problem Set 2 - 2.1, 2.6, 2.11, 2.26, 2.34, 2.35

2.1 (a) $\Delta H_{vap} = 2447 \text{kJ/kg}$, then

$$q = (1 \text{ L H}_2\text{O}) \left(\frac{1 \text{ kg H}_2\text{O}}{1 \text{ L}}\right) (2447 \text{ kJ/kg}) = 2447 \text{ kJ}$$

(b) $C_{\text{H}_2\text{O}} = 4 \,\text{J}/^{\circ}\text{C} \cdot \text{g} = 4 \,\text{kJ}/^{\circ}\text{C} \cdot \text{g},$

$$(2447 \text{ kJ}) \left(\frac{1^{\circ} C \cdot \text{kg}}{4 \text{ kJ}} \right) \left(\frac{1 \text{ hiker}}{60 \text{ kg}} \right) = 10^{\circ} C$$

(c) $C_{12}H_{22}O_{11}(g) + 12O_2(g) \rightarrow 12CO_2(g) + 11H_2O(l)$

 $\Delta H = \{11(-285.8 \,\mathrm{kJ/mol}) + 12(-393.5 \,\mathrm{kJ/mol})\} - \{-2222.1 \,\mathrm{kJ/mol}\} = -5644 \,\mathrm{kJ/mol}\}$

The molecular weight of sucrose is 12(12 g/mol) + 22(1 g/mol) + 11(16 g/mol) = 342 g/mol, then

$$2447\,\mathrm{kJ}\left(\frac{1\,\mathrm{mol\,sucrose}}{5644\,\mathrm{kJ}}\right)\left(\frac{342\,\mathrm{g}}{1\,\mathrm{mol}}\right) = 148\,\mathrm{g}$$

2.6 (a) 100 g $H_2O(l)$ heated from $T = 0^{\circ}C \rightarrow 100^{\circ}C$ at 1 atm,

$$C_p^{(H_2O)} = 4 \,\mathrm{J/^{\circ}C \cdot g}$$

$$q = (100 \,\mathrm{g})(100^{\circ}C - 0^{\circ}C)(4 \,\mathrm{J/^{\circ}C \cdot g}) = 40 \,\mathrm{kJ}$$

which is positive, since heat is put in.

(b) 100 g $H_2O(l)$ frozen at $0^{\circ}C$ at 0.01 atm

$$\Delta H_{\text{fusion}}^{(H_2O)} = (6 \,\text{kJ/mol}) \left(\frac{1 \,\text{mol}}{18 \,\text{g}}\right) = 333 \,\text{J}$$

Since we are freezing the water, by convention the sign is negative (taking heat out), and

$$q = (-333 \,\mathrm{J/g})(100 \,\mathrm{g}) = -33.3 \,\mathrm{kJ}$$

(c) $100 \text{ g } H_2O(l)$ evaporated to steam at $100^{\circ}C$, 1 atm,

$$\Delta H_{\text{vap}}^{(H_2O)} = (40.7 \,\text{kJ/mol}) \left(\frac{1 \,\text{mol}}{18 \,\text{g}}\right) = 2.26 \,\text{kJ/g}$$

$$q = (2.26 \,\mathrm{kJ/g})(100 \,\mathrm{g}) = 226 \,\mathrm{kJ}$$

2.11 1 mol $H_2O(l)$ at $100^{\circ}C$, heated until completely vaporaized. Calcuate $q, w, \Delta E, \Delta H$.

(a) In a cylinder, $p_{ex} = 1$ atm

$$V_{gas} = \frac{nRT}{p} = \frac{(1 \text{ mol})(8.2 \times 10^{-2} \text{ L} \cdot atm/K \cdot \text{mol})(373K)}{(1atm)} = 30.6 \text{ L}$$

$$V_{liquid} = (1 \text{ mol } H_2O) \left(\frac{18 \text{ g}}{1 \text{ mol}}\right) \left(\frac{10^{-3} \text{ L}}{1 \text{ g}}\right) = 0.018 \text{ L} \approx 0$$

$$w = -p_{ex}\Delta V = -(1 \text{ atm})(30.6 \text{ L}) \left(\frac{101 \text{ J}}{\text{L} \cdot \text{atm}}\right) = -3.09 \text{ kJ}$$

$$\Delta E = q + w = (-3.09 \text{ kJ}) + (40.7 \text{ kJ}) = 37.6 \text{ kJ}$$

$$\Delta H = q_{p=const} = 40.7 \text{ kJ}$$

$$w = 0 \leftarrow \text{expansion against a vacuum}$$

Since ΔE and ΔH are state functions, they are path independent, and so we may use the values from the previous section, giving

$$\Delta E = 37.6 \,\text{kJ} = q; \Delta H = 40.7 \,\text{kJ}$$

2.26 (a) $C_6H_{12}O_6(s) \rightarrow 2CH_3CH_2OH(l) + 2CO_2(g)$

$$\Delta H_{rxn} = \sum \Delta H(products) - \sum \Delta H(reactants)$$

$$\Delta H_{rxn}^{EtOH} = \left\{ 2 (-277\,\mathrm{kJ/mol}) + 2 (-394\,\mathrm{kJ/mol}) \right\} - \left\{ -1274\,\mathrm{kJ/mol} \right\} = -68\,\mathrm{kJ/mol}$$

(b)
$$C_6H_{12}O_6(s) + 2O_2(g) \rightarrow 2CH_3COOH(l) + 2CO_2(g) + 2H_2O(l)$$

$$\Delta H_{rxn}^{AcOH} = \left\{ 2(-484\,\mathrm{kJ/mol}) + 2(-394\,\mathrm{kJ/mol}) + 2(-286\,\mathrm{kJ/mol}) \right\} - \left\{ -1274\,\mathrm{kJ/mol} \right\} = -1054\,\mathrm{kJ/mol}$$

(c)
$$C_6H_{12}O_6(s) + 6O_2(g) \rightarrow 6CO_2(g) + 6H_2O(l)$$

$$\Delta H_{rxn}^{combust} = \{6(-394\,\mathrm{kJ/mol}) + 6(-286\,\mathrm{kJ/mol})\} - \{-1274\,\mathrm{kJ/mol}\} = -2806\,\mathrm{kJ/mol}\}$$

2.34 (a) *n*-octane, $8C(graphite) + 9H_2 \rightarrow C_8H_{18}(g)$

$$\Delta H_f = \{8(C - C graphite) + 9(H - H)\} - \{7(C - C) + 18(C - H)\}\$$

Remember, it takes energy to break bonds (by convention, +) and energy is released when bonds are made (by convention, -). Substituting in the appropriate values,

$$\Delta H_f = \{8(717\,\mathrm{kJ/mol}) + 9(436\,\mathrm{kJ/mol})\} - \{7(344\,\mathrm{kJ/mol}) + 18(415\,\mathrm{kJ/mol})\} = -218\,\mathrm{kJ/mol}\} = -218\,\mathrm{kJ/mol}\}$$

The experimental value is $-208 \,\mathrm{kJ/mol}$, which is pretty good, considering the approximation of using average bond enthalpies.

(b) Naphthalene, $10C(graphite) + 4H_2(g) \rightarrow C_{10}H_8(g)$

$$\Delta H_f = \{10(C - C graphite) + 4(H - H)\} - \{5(C = C) + 6(C - C) + 8(C - H)\}$$

$$\Delta H_f = \{10(717\,\mathrm{kJ/mol}) + 4(436\,\mathrm{kJ/mol})\} - \{5(615\,\mathrm{kJ/mol}) + 6(344\,\mathrm{kJ/mol}) + 8(415\,\mathrm{kJ/mol})\} = +455\,\mathrm{kJ/mol}\} + 4(436\,\mathrm{kJ/mol})\} - \{5(615\,\mathrm{kJ/mol}) + 6(344\,\mathrm{kJ/mol}) + 8(415\,\mathrm{kJ/mol})\} = +455\,\mathrm{kJ/mol}\} = +455\,\mathrm{kJ/mol}\} + 4(436\,\mathrm{kJ/mol}) + 4(436\,\mathrm{kJ/mol})\} = +455\,\mathrm{kJ/mol}\} = +455\,\mathrm{kJ/mol}$$

 $\Delta H_{exptl} = +151 \,\mathrm{kJ/mol}$, since naphthalene is more stable due to resonance effects.

(c) Formaldehyde, $C(graphite) + H_2 + 1/2 O_2 \rightarrow H_2 C = O$

$$\Delta H_f = \{ (717 \,\mathrm{kJ/mol}) + (436 \,\mathrm{kJ/mol}) + 1/2 \,(498 \,\mathrm{kJ/mol}) \} - \{ 2(415 \,\mathrm{kJ/mol}) + (725 \,\mathrm{kJ/mol}) \} = -153 \,\mathrm{kJ/mol} \} = -153 \,\mathrm{kJ/mol} \} = -153 \,\mathrm{kJ/mol} \}$$

 $\Delta H_{exptl} = -116\,\mathrm{kJ/mol}$, the average-bond enthalpy appoximation is most valid in the large-molecule limit.

(d) Formic acid, $C(graphite) + H_2 + O_2 \rightarrow HCOOH$

$$\Delta H_f = \{(717\,\mathrm{kJ/mol}) + (436\,\mathrm{kJ/mol}) + (498\,\mathrm{kJ/mol})\} - \{(415\,\mathrm{kJ/mol}) + (725\,\mathrm{kJ/mol}) + (350\,\mathrm{kJ/mol}) + (463\,\mathrm{kJ/mol})\} - \{(415\,\mathrm{kJ/mol}) + (350\,\mathrm{kJ/mol}) + (350\,\mathrm{kJ/mol}) + (463\,\mathrm{kJ/mol})\} - \{(415\,\mathrm{kJ/mol}) + (350\,\mathrm{kJ/mol}) + (350\,\mathrm{$$

 $\Delta H_f = -302 \,\mathrm{kJ/mol}$, $\Delta H_{exptl} = -379 \,\mathrm{kJ/mol}$, discrepancy due to resonance effects, with the hydroxyl hydrogen capable of being on either oxygen.

2.35 cis-2-butene $\rightarrow trans$ -2-butene

$$\Delta H_{cis \rightarrow trans} = \Delta H_f^{(trans)} - \Delta H_f^{(cis)} = (-11.1\,\mathrm{kJ/mol}) - (-7.0\,\mathrm{kJ/mol}) = -4.1\,\mathrm{kJ/mol}$$

So we see that the trans configuration is more stable than the cis configuration, this is known as the "trans-effect".